

GLOBAL EKSEN TAKIMINDA ELEMAN STİFNES (RİJİTLİK) MATRİS TABLOSU

(x-y Düzlemindeki doğru eksenli prizmatik j çubuk elemanı için)

$$(s_j) = \begin{bmatrix} s(1,1) & s(1,2) & s(1,3) & (-) & (-) & (+) \\ s(2,1) & s(2,2) & s(2,3) & (-) & (-) & (+) \\ s(3,1) & s(3,2) & s(3,3) & (-) & (-) & \frac{1}{2}(+) \\ \hline (-) & (-) & (-) & (+) & (+) & (-) \\ (-) & (-) & (-) & (+) & (+) & (-) \\ (+) & (+) & \frac{1}{2}(+) & (-) & (-) & (+) \end{bmatrix}$$

Sol üst köşedeki tablo elemanları aşağıda tarif edilmektedir. Tabloda verilen katsayı ve işaretlerle aşağıda tarif edilen tablo elemanları çarpılarak tablonun diğer elemanları elde edilir.

$$s(1,1) = (E_j A_j / L_j) (\cos \alpha_j)^2 + (12 E_j I_j / L_j^3) (\sin \alpha_j)^2$$

$$s(1,2) = [(E_j A_j / L_j) - (12 E_j I_j / L_j^3)] (\cos \alpha_j \cdot \sin \alpha_j)$$

$$s(1,3) = -(6 E_j I_j / L_j^2) (\sin \alpha_j)$$

$$s(2,1) = s(1,2)$$

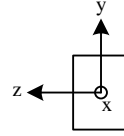
$$s(2,2) = (E_j A_j / L_j) (\sin \alpha_j)^2 + (12 E_j I_j / L_j^3) (\cos \alpha_j)^2$$

$$s(2,3) = (6 E_j I_j / L_j^2) (\cos \alpha_j)$$

$$s(3,1) = s(1,3)$$

$$s(3,2) = s(2,3)$$

$$s(3,3) = (4 E_j I_j / L_j)$$



α_j = Elemanın Referans Açısı

A_j = Elemanın Dik Kesit Alanı

I_j = Elemanın Asal Atalet Momenti (z eksenine göre)

L_j = Elemanın Boyu

E_j = Elemanın Malzeme Elastisite Modülü

ÖZEL HALLER

Kiriş Elemanı ($\alpha_j = 0$)

(Referans noktası sol uçta)

$$s(1,1) = (E_j A_j / L_j)$$

$$s(1,2) = 0$$

$$s(1,3) = 0$$

$$s(2,1) = 0$$

$$s(2,2) = (12 E_j I_j / L_j^3)$$

$$s(2,3) = (6 E_j I_j / L_j^2)$$

$$s(3,1) = 0$$

$$s(3,2) = (6 E_j I_j / L_j^2)$$

$$s(3,3) = (4 E_j I_j / L_j)$$

Kolon Elemanı ($\alpha_j = 90$)

(Referans noktası alt uçta)

$$s(1,1) = (12 E_j I_j / L_j^3)$$

$$s(1,2) = 0$$

$$s(1,3) = -(6 E_j I_j / L_j^2)$$

$$s(2,1) = 0$$

$$s(2,2) = (E_j A_j / L_j)$$

$$s(2,3) = 0$$

$$s(3,1) = -(6 E_j I_j / L_j^2)$$

$$s(3,2) = 0$$

$$s(3,3) = (4 E_j I_j / L_j)$$

Kafes Elemanı ($I_j = 0$)

(S matrisindeki tüm $I_j = 0$)

$$s(1,1) = (E_j A_j / L_j) (\cos \alpha_j)^2$$

$$s(1,2) = (E_j A_j / L_j) (\cos \alpha_j \cdot \sin \alpha_j)$$

$$s(1,3) = 0$$

$$s(2,1) = (E_j A_j / L_j) (\cos \alpha_j \cdot \sin \alpha_j)$$

$$s(2,2) = (E_j A_j / L_j) (\sin \alpha_j)^2$$

$$s(2,3) = 0$$

$$s(3,1) = 0$$

$$s(3,2) = 0$$

$$s(3,3) = 0$$

Eleman eksen takımındaki çubuk ucu kuvvetleri $[q_j^1]$ 'lerin, global eksen takımındaki düğüm noktası deplasmanları

$[d_j]$ 'ler cinsinden tarifleri

$$q_{j1}^1 = -(E_j A_j / L_j) [(d_{j4} - d_{j1}) (\cos \alpha_j) + (d_{j5} - d_{j2}) (\sin \alpha_j)]$$

$$q_{j2}^1 = (E_j I_j / L_j^2) \left[6d_{j3} + 6d_{j6} - \frac{12}{L_j} [(d_{j5} - d_{j2}) (\cos \alpha_j) - (d_{j4} - d_{j1}) (\sin \alpha_j)] \right]$$

$$q_{j3}^1 = (E_j I_j / L_j) \left[4d_{j3} + 2d_{j6} - \frac{6}{L_j} [(d_{j5} - d_{j2}) (\cos \alpha_j) - (d_{j4} - d_{j1}) (\sin \alpha_j)] \right]$$

$$q_{j4}^1 = (E_j A_j / L_j) [(d_{j4} - d_{j1}) (\cos \alpha_j) + (d_{j5} - d_{j2}) (\sin \alpha_j)]$$

$$q_{j5}^1 = -(E_j I_j / L_j^2) \left[6d_{j3} + 6d_{j6} - \frac{12}{L_j} [(d_{j5} - d_{j2}) (\cos \alpha_j) - (d_{j4} - d_{j1}) (\sin \alpha_j)] \right]$$

$$q_{j6}^1 = (E_j I_j / L_j) \left[2d_{j3} + 4d_{j6} - \frac{6}{L_j} [(d_{j5} - d_{j2}) (\cos \alpha_j) - (d_{j4} - d_{j1}) (\sin \alpha_j)] \right]$$

ÖZEL HALLER

Kiriş Elemanı ($\alpha_j = 0$)

$$q'_{j1} = -(E_j A_j / L_j)(d_{j4} - d_{j1})$$

$$q'_{j2} = (E_j I_j / L_j^2) \left[6d_{j3} + 6d_{j6} - \frac{12}{L_j}(d_{j5} - d_{j2}) \right]$$

$$q'_{j3} = (E_j I_j / L_j) \left[4d_{j3} + 2d_{j6} - \frac{6}{L_j}(d_{j5} - d_{j2}) \right]$$

$$q'_{j4} = (E_j A_j / L_j)(d_{j4} - d_{j1})$$

$$q'_{j5} = -(E_j I_j / L_j^2) \left[6d_{j3} + 6d_{j6} - \frac{12}{L_j}(d_{j5} - d_{j2}) \right]$$

$$q'_{j6} = (E_j I_j / L_j) \left[2d_{j3} + 4d_{j6} - \frac{6}{L_j}(d_{j5} - d_{j2}) \right]$$

Kafes Elemanı ($I_j = 0$)

$$q'_{j1} = -(E_j A_j / L_j) \left[(d_{j4} - d_{j1})(\cos \alpha_j) + (d_{j5} - d_{j2})(\sin \alpha_j) \right]$$

$$q'_{j2} = 0$$

$$q'_{j3} = 0$$

$$q'_{j4} = (E_j A_j / L_j) \left[(d_{j4} - d_{j1})(\cos \alpha_j) + (d_{j5} - d_{j2})(\sin \alpha_j) \right]$$

$$q'_{j5} = 0$$

$$q'_{j6} = 0$$

Kolon Elemanı ($\alpha_j = 90$)

$$q'_{j1} = -(E_j A_j / L_j)(d_{j5} - d_{j2})$$

$$q'_{j2} = (E_j I_j / L_j^2) \left[6d_{j3} + 6d_{j6} + \frac{12}{L_j}(d_{j4} - d_{j1}) \right]$$

$$q'_{j3} = (E_j I_j / L_j) \left[4d_{j3} + 2d_{j6} + \frac{6}{L_j}(d_{j4} - d_{j1}) \right]$$

$$q'_{j4} = (E_j A_j / L_j)(d_{j5} - d_{j2})$$

$$q'_{j5} = -(E_j I_j / L_j^2) \left[6d_{j3} + 6d_{j6} + \frac{12}{L_j}(d_{j4} - d_{j1}) \right]$$

$$q'_{j6} = (E_j I_j / L_j) \left[2d_{j3} + 4d_{j6} + \frac{6}{L_j}(d_{j4} - d_{j1}) \right]$$

j çubuk elemanı üzerine etki eden (w_j , P_j , N_j , M_j) yüklerine bağlı eleman eksen takımındaki çubuk ucu kuvvetleri

$\left[\bar{q}'_j \right]$ 'lerin tarifi

$$\bar{q}'_{j1} = \frac{b_j N_j}{L_j}$$

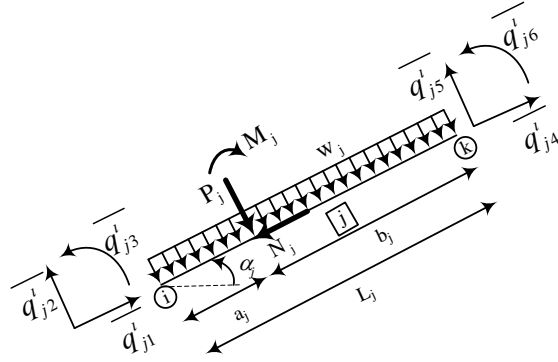
$$\bar{q}'_{j2} = \frac{w_j L_j}{2} + \frac{P_j b_j^2 (3a_j + b_j)}{L_j^3} - \frac{6M_j a_j b_j}{L_j^3}$$

$$\bar{q}'_{j3} = \frac{w_j L_j^2}{12} + \frac{P_j b_j^2 a_j}{L_j^2} + \frac{M_j b_j (b_j - 2a_j)}{L_j^2}$$

$$\bar{q}'_{j4} = \frac{a_j N_j}{L_j}$$

$$\bar{q}'_{j5} = \frac{w_j L_j}{2} + \frac{P_j a_j^2 (3b_j + a_j)}{L_j^3} + \frac{6M_j a_j b_j}{L_j^3}$$

$$\bar{q}'_{j6} = -\frac{w_j L_j^2}{12} - \frac{P_j a_j^2 b_j}{L_j^2} + \frac{M_j a_j (a_j - 2b_j)}{L_j^2}$$



Global eksen takımındaki çubuk ucu kuvvetleri $\left[\bar{q}_j \right]$ 'lerin yukarıda tarif edilen $\left[\bar{q}'_j \right]$ 'ler cinsinden ifadeleri

Genel Elemanı

$$\bar{q}_{j1} = \bar{q}'_{j1} (\cos \alpha_j) - \bar{q}'_{j2} (\sin \alpha_j)$$

$$\bar{q}_{j2} = \bar{q}'_{j1} (\sin \alpha_j) + \bar{q}'_{j2} (\cos \alpha_j)$$

$$\bar{q}_{j3} = \bar{q}'_{j3}$$

$$\bar{q}_{j4} = \bar{q}'_{j4} (\cos \alpha_j) - \bar{q}'_{j5} (\sin \alpha_j)$$

$$\bar{q}_{j5} = \bar{q}'_{j4} (\sin \alpha_j) + \bar{q}'_{j5} (\cos \alpha_j)$$

$$\bar{q}_{j6} = \bar{q}'_{j6}$$

Kiriş Elemanı ($\alpha_j = 0$)

$$\bar{q}_{j1} = \bar{q}'_{j1}$$

$$\bar{q}_{j2} = \bar{q}'_{j2}$$

$$\bar{q}_{j3} = \bar{q}'_{j3}$$

$$\bar{q}_{j4} = \bar{q}'_{j4}$$

$$\bar{q}_{j5} = \bar{q}'_{j5}$$

$$\bar{q}_{j6} = \bar{q}'_{j6}$$

Kolon Elemanı ($\alpha_j = 90$)

$$\bar{q}_{j1} = -\bar{q}'_{j2}$$

$$\bar{q}_{j2} = \bar{q}'_{j1}$$

$$\bar{q}_{j3} = \bar{q}'_{j3}$$

$$\bar{q}_{j4} = -\bar{q}'_{j5}$$

$$\bar{q}_{j5} = \bar{q}'_{j4}$$

$$\bar{q}_{j6} = \bar{q}'_{j6}$$